Unsteady Blade Pressures on a Propfan at Takeoff: Euler Analysis and Flight Data

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The unsteady blade pressures due to the operation of the propfan at an angle to the direction of the mean flow are obtained by solving the unsteady three-dimensional Euler equations. The configuration considered is the eight-bladed SR7L propfan operating at takeoff conditions, and the inflow angles considered are 6.3, 8.3, and 11.3 deg. The predicted blade pressure waveforms are compared with in-flight measurements. At the inboard radial station (r/R = 0.68) the phase of the predicted waveforms show reasonable agreement with measurements, whereas, the amplitudes are overpredicted in the leading-edge region of the blade. At the outboard radial station (r/R = 0.95), the predicted amplitudes of the waveforms on the pressure surface are in good agreement with flight data for all inflow angles. The measured (installed propfan) waveforms show a relative phase lag compared to the computed (propfan alone) waveforms. The phase lag depends on the axial location of the transducer and the surface of the blade. On the suction surface, in addition to the relative phase lag, the measurements show distortion (widening and steepening) of the waveforms. The extent of distortion increases with increase in inflow angle. This distortion seems to be due to viscous separation effects which depends on the azimuthal location of the blade and the axial location of the transducer.

Introduction

THE enhanced fuel efficiency characteristics of the propfans over the conventional propellers were demonstrated by NASA through its advanced turboprop project. Further improvement in fuel efficiency, noise reduction, and structures may result only from a better understanding of the flow features at the design and off-design operating conditions. This understanding is crucial to the improvement of design methodologies for future propfan design.

Flight measurements on a large-scale 9-ft (2.74-m) diameter SR7L propfan have provided a unique data base of blade stresses, near-field sound pressure levels, and blade surface pressures over a range of operating conditions.^{2,3} This data base may be used to understand the propfan aerodynamic characteristics, validate prediction methods, and improve design methodologies. In the flight tests, the propfan was installed on the left wing of a modified instrumented Gulfstream II test-bed aircraft. A nacelle tilt arrangement was used to vary the inflow angle to the propfan. Three nacelle tilt angles were considered, -3 and -1 deg (tilt down) and +2 deg (tilt up). The effective inflow angle α to the propfan, however, depends on the airplane angle of attack, nacelle tilt, and upwash angle of the flow into the propfan.

The detailed in-flight unsteady blade pressure measurements were made on a specially designed instrumented blade using 30 transducers.³ The blade suction surface had 20 pressure transducers distributed over three radial stations (r/R = 0.68, 0.86, and 0.95), where r is the radial distance and R is the blade tip radius) while the pressure surface had 10 pressure transducers distributed over two radial stations (r/R = 0.68 and 0.95). The axial positions of the transducers from the blade leading edge are listed in Table 1 in terms of normalized chord length, x/c where x is the axial distance and c is the blade chord. Tests were carried out over a range of takeoff and cruise operating conditions.

The unsteady flow features of a propfan at cruise operating conditions were examined by Nallasamy and Groeneweg.⁴ They showed that at inflow angles of the order of 5 deg, strong passage shocks extending from suction to pressure surface form and dissolve during each revolution of the blade. They also studied the unsteady flow effects on the blade loading and pressure waveforms at takeoff conditions for an inflow angle of 8.3 deg (corresponding to a nacelle tilt of -1 deg),⁵ and compared with in-flight measurements. The predicted blade pressure waveforms showed reasonable agreement with flight data at the inboard radial station (r/R = 0.68), whereas, at the outboard radial station (r/R = 0.95) the agreement was poor.

In this article the effect of inflow angle on the blade pressure at takeoff operating conditions, Mach number M=0.31 and advance ratio J=1.6 is further studied by obtaining unsteady three-dimensional Euler solution for 6.3- and 11.3-deg inflow angles corresponding to nacelle tilt angles of -3 and +2 deg, respectively, of the flight test.³ The results obtained here are analyzed together with that obtained for 8.3 deg,⁵ to understand the effect of inflow angle on the blade loading and blade pressure waveforms. The predicted blade pressure waveforms are compared with flight measurements.

Numerical Solution of Unsteady, Three-Dimensional Euler Equations

The unsteady three-dimensional Euler equations governing the inviscid flow through a propfan are solved employing a solution procedure developed by Whitfield et al.^{6,7} In this procedure the Euler equation in conservative differential form are transformed from a Cartesian reference frame to a body-fitted curvilinear reference frame. Then the transformed equations are discretized employing a finite-volume technique. An approximate Riemann solver is used for block in-

Table 1 Unsteady pressure blade transducer locations in flight test³

$\frac{\text{Radius, } r/R}{0.68}$	Surface Suction Pressure	Normalized chord, x/c						
		0.05	0.10	0.15 0.15	0.25		0.60 0.60	
0.68	Suction		0.15	0.25		0.50	0.75	0.90
0.95	Suction Pressure	$0.08 \\ 0.08$				0.58 0.58		

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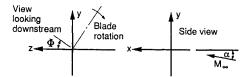


Fig. 1 Reference coordinates.

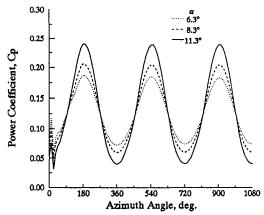


Fig. 2 Power per blade variation with azimuth angle, M = 0.31, J = 1.6.

terface flux definitions and a lower-upper (LU) implicit numerical scheme is used to solve the discretized equations. The flowfield is represented by multiblock composite grid to limit the core memory requirements.

Flow Configuration and Computational Grid

The configuration considered here is that of the eight-bladed SR7L propfan of the flight test.³ The direction of rotation of the propfan and the axes of reference are shown in Fig. 1. The rotation of the propfan is clockwise, looking downstream, and the azimuth angle Φ is measured from the z axis as shown. The blade design hot coordinates were used to generate the grid. The grid employed here to represent the flowfield is the same as that shown in Fig. 2 of Ref. 5. An H-grid, with 107 \times 41 \times 13 (axial by radial by circumferential) points in each blade passage is employed. Each blade passage is divided into three blocks with $107 \times 41 \times 5$ grid points in each block. Therefore, 24 blocks of grid were used to describe the entire flowfield with 456,248 nodal points. Each blade surface is represented by 49×27 (axial by spanwise) grid points with higher resolution near the leading and trailing edges, the hub and the tip. Similar grids used with the present solution technique have produced results which are in reasonably good agreement with data.8,9

Results and Discussion

The unsteady three-dimensional Euler solutions were obtained for the following two flight tests cases of Ref. 3: 1) run = 187, and nacelle tilt = -3 deg; and 2) run = 113, and nacelle tilt = +2 deg. The takeoff operating conditions, Mach number = 0.31 and advance ratio = 1.6, are considered. The aircraft angle of attack for these test cases was 5.4 deg. In addition to nacelle tilt angle and aircraft angle of attack, the upwash angle at the propfan is needed to determine the effective inflow angle.

In the absence of a simple computational procedure to determine the upwash angle, an experimental correlation obtained by Heidelberg and Woodward¹⁰ from their SR7A model propfan test in the NASA Lewis 9 by 15-ft wind tunnel was used to estimate the inflow angle to the propfan. They first measured the pressure response of the blades as a function of inflow angle for the propfan-alone configuration. Then a wing was installed downstream of the propfan (as in the flight test case, tractor configuration) and blade pressure response was measured over a range of wing angles of attack and nacelle tilt. It is assumed that the local inflow angle and the propfan angle of attack are the same in the propfan-alone case. Then

by matching the measured first harmonic response of the blades with wing installation to that of propfan-alone configuration, they found the equivalent inflow angle as a function of wing angle of attack (Fig. 13 in Ref. 8). This correlation was obtained for takeoff conditions, Mach number = 0.2, advance ratio = 0.88, and with a straight wing. The same correlation is used here to obtain the effective inflow angle to the propfan. For an aircraft (wing) angle of attack of 5.4 deg, a nacelle tilt (droop) angle of -3 deg gives a value of 6.3 deg for the effective inflow angle α (Fig. 1), whereas, a nacelle tilt of +2 deg gives a value of 11.3 deg.

The Euler solutions reported here were obtained with inflow angles of 6.3 and 11.3 deg giving an inflow variation of 5 deg for a 5-deg change in nacelle tilt. These solutions are examined together with that obtained for an inflow angle of 8.3 deg (nacelle tilt = -1 deg) in Ref. 5, at the same takeoff operating conditions. The present solutions were obtained from an impulse start for three complete revolutions of the propfan, to obtain a reasonably accurate solution. By the third revolution, the results have stabilized as indicated by the periodic variation of per blade power coefficient during the second and third revolutions of the propfan, Fig. 2. The figure shows the variation of the power coefficient with azimuth angle for three inflow angles, for a blade starting at $\Phi = 0$ and executing three complete revolutions ($\Phi = 0$ to 1080 deg). The results of the third revolution are analyzed and presented here. The predicted total power coefficients (for eight blades) are nearly the same for all three inflow angles and are about 1% higher than the measured value. The expected sinusoidal variation of the blade loading due to inflow angle is clearly observed in all cases. The amplitude of the stabilized power coefficient during the third revolution varies +44 and -42% about the mean for $\alpha = 6.3$ deg, +61 and -53% for $\alpha = 8.3$ deg, and +89 and -68% for $\alpha = 11.3$ deg. For the low inflow angle ($\alpha = 6.3$ deg) the variation about the mean in the positive and negative directions is nearly the same, as it was also observed in Refs. 5 and 9. For higher inflow angles, the difference between the minimum and maximum levels about the mean results directly from the higher positive inflow angles, as a look at the velocity triangles would show.

The harmonic content of the blade loading is obtained by Fourier transforming the blade power coefficient variation during the third revolution of the blade. The power coefficient $C_p = a_0 + a_i \cos \omega t + b_i \sin \omega t$, where a_0 , a_i , b_i are the Fourier coefficients and t is the time. The loading spectra are shown in Fig. 3. It is seen that the predicted mean blade power coefficient is nearly the same for all three inflow angles, and the first harmonic dominates the blade loading. The first harmonic loading lags the blade motion by 3.62, 3.68, and 3.75 deg for the three inflow angles, 6.3, 8.3, and 11.3 deg, respectively. The relatively low value of lag and the smaller variation with inflow angle are due to the low reduced frequency and flow unsteadiness at the takeoff operating conditions considered here.

The azimuthal variation of the power coefficient $dC_p/d(r/R)$ are shown in Fig. 4. Figure 4a shows the computed elemental

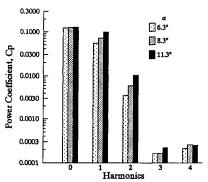


Fig. 3 Loading spectra, M = 0.31, J = 1.6.

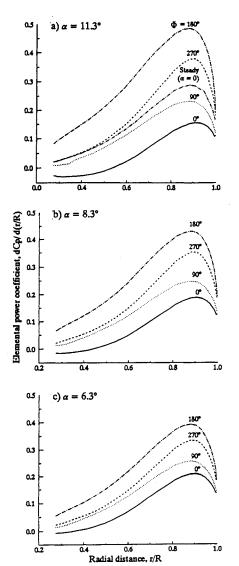


Fig. 4 Elemental power coefficient variation during a revolution, M = 0.31, J = 1.6.

power coefficient variation for an inflow angle of 11.3 deg at four azimuthal locations, $\Phi = 0$, 90, 180, and 270 deg. Also shown in the figure is the curve for the steady flow $(\alpha = 0)$ deg). The shape of the curve for any azimuthal position is similar to that of the steady flow. The magnitude of the cyclic variation depends on the spanwise location. At $\Phi = 180$ and 270 deg locations, the loading levels are higher than the steady $(\alpha = 0)$ values, whereas at $\Phi = 0$ and 90 deg they are lower than the steady ones. The elemental power coefficient variation for an inflow angle of 8.3 deg is shown in Fig. 4b. The trends of the curves with azimuth angle are similar to that of 11.3 deg; higher loading levels occur for $\Phi = 180$ and 270 deg, and lower loading levels for $\Phi = 0$ - and 90-deg positions. Figure 4c shows the elemental power coefficient variations for $\alpha = 6.3$ deg. The magnitude of the cyclic variation is small for this inflow angle. At any inflow angle, the maximum deviation (in absolute value) from the steady value occurs at the radial station where the elemental power coefficient attains a maximum, as would be expected from angle-of-attack variations along the blade span.

The comparisons of the predicted blade pressure waveforms with flight data are presented next for two inflow angles $\alpha=6.3$ and 11.3 deg. Such comparisons for $\alpha=8.3$ deg were reported in Ref. 5 and reference to it would be made where appropriate. In these waveform comparisons, 0 deg corresponds to the (top-dead-center) vertical direction for aircraft installation as in the presentation of flight data in Ref. 3. At the outset, it should be mentioned that for the takeoff op-

erating conditions considered here, the flight data do not indicate the formation of a leading-edge vortex. During the flight test no steady measurements were made. However, some steady pressure data were obtained during the unsteady pressure test by retaining the dc component of the pressure signal. These data do not indicate the formation of a leading-edge vortex. When a leading-edge vortex is present, the pressure wave forms on the suction surface show double hump form which is absent in the measured waveforms for the present cases, thus, suggesting the absence of the vortex (see the waveforms and discussion below).

Figure 5 shows the unsteady blade surface pressure as a function of azimuth angle for the transducer locations on the suction surface at r/R=0.68 for $\alpha=6.3$ deg. The measured and predicted waveforms indicate that the response is the largest near the leading edge and the response reduces gradually towards the trailing edge. The predicted phases of the waveforms are in close agreement with data. However, the amplitudes are overpredicted, the maximum overprediction in absolute value occurring near the leading edge. The pressure waveforms for the four transducer locations on the pressure surface at this radial station are shown in Fig. 6. Here again, the phases of the predicted waveforms agree quite well while the amplitudes are overpredicted.

The pressure waveforms at the outboard radial station r/R = 0.95 for $\alpha = 6.3$ deg are shown in Figs. 7 and 8. Figure 7 shows the pressure waveforms on the suction surface. Even at this radial station, the prediction shows that the largest response occurs near the leading edge and reduce gradually towards the trailing edge. The measurements, however, indicate that the maximum response occurs at x/c = 0.42. For this and the transducer at x/c = 0.58, the magnitudes are severely underpredicted. The measured waveform is distorted from the linear sinusoidal form of the predicted one. The waveform distortion may occur due to viscous effects manifesting in the form of a small separation bubble as suggested

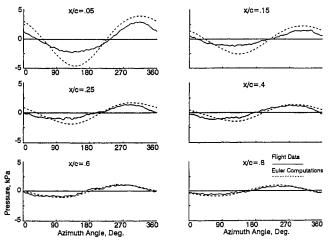


Fig. 5 Pressure waveforms on the suction surface at r/R = 0.68, $\alpha = 6.3$ deg.

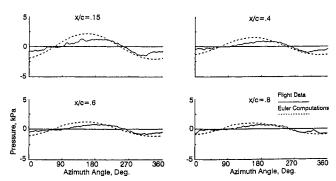


Fig. 6 Pressure waveforms on the pressure surface at r/R = 0.68, $\alpha = 6.3$ deg.

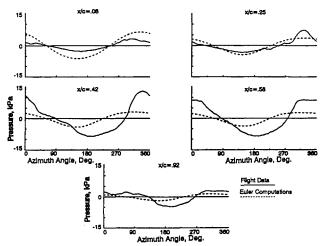


Fig. 7 Pressure waveforms on the suction surface at r/R = 0.95, $\alpha = 6.3$ deg.

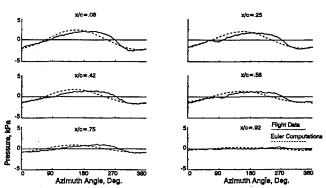


Fig. 8 Pressure waveforms on the pressure surface at r/R = 0.95, $\alpha = 6.3$ deg.

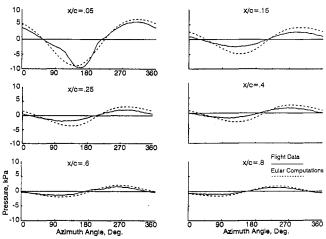


Fig. 9 Pressure waveforms on the suction surface at r/R = 0.68, $\alpha = 11.3$ deg.

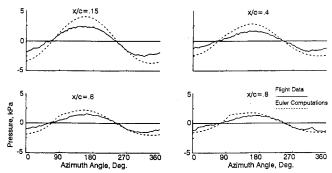


Fig. 10 Pressure waveforms on the pressure surface at r/R = 0.68, $\alpha = 11.3$ deg.

by the low pressure (within the bubble) at $\Phi \sim 180$ deg for x/c = 0.42 and 0.58, and steep rise in pressure (outside the bubble) at about $\Phi = 270$ deg. The phases of the waveform also differ from the flight data. For all the transducer locations, the measured waveform shows a relative phase lag compared to the Euler solution. This phase lag also attains a maximum at x/c = 0.42. This phase lag seems to be the result of installation effect, that is, the presence of the wing in the flight tests as compared to the propfan-alone configuration of the computation. Heidelberg and Woodward¹⁰ noted similar phase variations in their model tests in the wind tunnel with and without wing installation. They show a relative phase lag of 11 deg with the wing installation for $\alpha = 10$ deg when compared to the propfan-alone case at a transducer location r/R = 0.75 and x/c = 0.1 on the suction surface of the model. whereas, the magnitudes are nearly the same. The phase lag observed here ranges from 4 deg near the leading edge (x/c)= 0.05) to about 60 deg at x/c = 0.42. On the pressure side (Fig. 8), however, the magnitudes are well-predicted, but the relative phase lag exists at all the transducer locations and it ranges from 15 to 50 deg. It should be noted here that the comparison of the waveforms predicted using the same solution technique with the propfan alone wind tunnel measured waveforms in Refs. 8 and 9 did not show any such phase lags.

The pressure waveforms for an inflow angle of 8.3 deg presented in Ref. 5 showed similar behavior at the outboard radial station. There the phase lag varied from 8 to 30 deg on the suction surface and from 20 to 38 deg on the pressure surface.

Next, the pressure waveforms for $\alpha=11.3$ deg are presented for the two radial stations. At the inboard radial station, both the predicted and measured pressure waveforms on the suction surface (Fig. 9) show that the maximum response occurs near the leading edge (x/c=0.05), and reduces gradually towards the trailing edge. At x/c=0.05 both magnitude and phase are in good agreement with flight measurements. At other transducer locations, the amplitude is overpredicted, the maximum overprediction occuring at x/c=0.15. On the pressure surface (Fig. 10), the predicted waveforms agree well in phase compared to measurements, although the amplitudes are overpredicted.

At the outboard radial station r/R = 0.95, the pressure waveforms on the suction surface are shown in Fig. 11 for $\alpha = 11.3$ deg. First, it is observed that the measured waveforms are distorted from sinusoidal form by broadening and steepening. This distortion increases with increase in inflow angle, 6.3-11.3 deg. At $\alpha = 11.3$ deg, the maximum distortion appears at x/c = 0.25 transducer location. As noted earlier, the distortion of the waveform may be the result of viscous separation. The measured waveform at x/c = 0.08 shows a relative phase lead compared to the computed (propfan-alone)

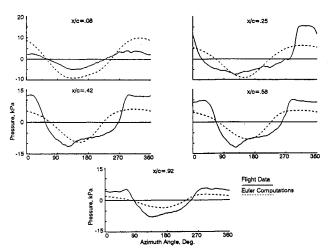


Fig. 11 Pressure waveforms on the suction surface at r/R = 0.95, $\alpha = 11.3$ deg.

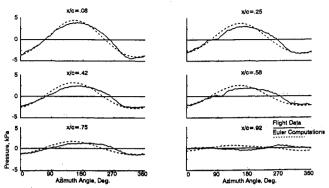


Fig. 12 Pressure waveforms on the pressure surface at r/R = 0.95, $\alpha = 11.3$ deg.

waveform, but at all other transducer locations a phase lag ranging from 15 to 55 deg is observed. On the pressure surface at this radial station, the predicted waveforms (Fig. 12) show very good agreement in magnitude with measurements (except at x/c = 0.92). But a relative phase lag of the measured waveforms ranging from 7 to 30 deg is observed. At x/c = 0.92 the blade response is low and the predicted waveform is 180 deg out of phase with that of flight measurement. This appears to be due to the strong interaction of the blade-wake and tip-vortex flows, and it is not clear as to the kind of interaction that would produce such a phase variation.

Concluding Remarks

The unsteady blade surface pressures due to the operation of the propfan at an angle to the mean flow direction were obtained by solving the three-dimensional Euler equations. Three positive inflow angles, $\alpha=6.3, 8.3,$ and 11.3 deg were considered. The predicted waveforms at the inboard radial station show reasonable agreement with in-flight measurements. At the outboard radial station, the measured waveforms show a relative phase lag compared to the predicted ones. This phase lag is due to the installation effects, i.e., the installed propfan of the flight test compared to the propfanalone configuration of the computation. On the suction surface the measured waveforms also show distortion (widening

and steepening) which increases with inflow angle. This distortion appears to be due to viscous effects which are not considered here. Higher flow resolution near the tip region and consideration of the viscous effects may improve the prediction at the outboard stations.

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